

Intuitionistic Fuzzy G_δ - e -locally Function

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ABSTRACT

The purpose of this paper is introduce the concepts of an intuitionistic fuzzy G_δ - e -locally function, intuitionistic fuzzy strongly G_δ - e -locally function, intuitionistic fuzzy G_δ - e -locally homeomorphism, intuitionistic fuzzy G_δ - e -locally irresolute function, intuitionistic fuzzy G_δ - e -local T_2 space, intuitionistic fuzzy G_δ - e -local Urysohn space, intuitionistic fuzzy G_δ - e -local connected, intuitionistic fuzzy G_δ - e -local compact in intuitionistic fuzzy topological spaces. Also some interesting properties are established.

KEYWORDS AND PHRASES: intuitionistic fuzzy G_δ - e - locally function, intuitionistic fuzzy strongly G_δ - e - locally function, intuitionistic fuzzy G_δ - e -local homeomorphism, intuitionistic fuzzy G_δ - e -local connected, intuitionistic fuzzy G_δ - e -local compact.

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1 INTRODUCTION

The concept of fuzzy sets was introduced by Zadeh [12] and later Atanassov [1] generalized the idea to intuitionistic fuzzy sets. On the other hand, Coker [3] introduced the notions of an intuitionistic fuzzy topological spaces, intuitionistic fuzzy continuity and some other related concepts. The concept of an intuitionistic fuzzy e -closed set was introduced by Sobana et. al., [10]. Ganster and Relly used locally closed sets in [5] to define LC-continuity and LC-irresoluteness. Balasubramanian [2] introduced and studied the concept of fuzzy G_δ set in a fuzzy topological space. In this paper, the concepts

of an intuitionistic fuzzy G_δ - e - locally function, intuitionistic fuzzy strongly G_δ - e -locally function, intuitionistic fuzzy G_δ - e -locally homeomorphism, intuitionistic fuzzy G_δ - e -locally irresolute function, intuitionistic fuzzy G_δ - e - local T_2 space, intuitionistic fuzzy G_δ - e - local Urysohn space, intuitionistic fuzzy G_δ - e - local connected, intuitionistic fuzzy G_δ - e - local compact are introduced and studied. Some interesting properties among these are discussed.

2 PRELIMINARIES

[1] Let X be a nonempty fixed set and I be the closed interval $[0,1]$. An intuitionistic fuzzy set (IFS) A is an object of the following form $A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$ where the mapping $\mu_A : X \rightarrow I$ and $\gamma_A : X \rightarrow I$ denote the degree of membership (namely $\mu_A(x)$) and the degree of nonmembership (namely $\gamma_A(x)$) for each element $x \in X$ to the set A , respectively, and $0 \leq \mu_A(x) + \gamma_A(x) \leq 1$ for each $x \in X$. Obviously, every fuzzy set A on a nonempty set X is an IFS of the following form, $A = \{ \langle x, \mu_A(x), 1 - \mu_A(x) \rangle : x \in X \}$. For the sake of simplicity, we shall use the symbol $A = \langle x, \mu_A, \gamma_A \rangle$ for the intuitionistic fuzzy set $A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$. [1] Let X be a nonempty set and the IFSs A and B in the form $A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$, $B = \{ \langle x, \mu_B(x), \gamma_B(x) \rangle : x \in X \}$. Then [(i)] $A \subseteq B$ if and only if $\mu_A(x) \leq \mu_B(x)$ and $\gamma_A(x) \geq \gamma_B(x)$ for all $x \in X$;

$$[(ii)] \bar{A} = \{ \langle x, \gamma_A(x), \mu_A(x) \rangle : x \in X \} \quad [(iii)]$$

$$A \cap B = \{ \langle x, \mu_A(x) \wedge \mu_B(x), \gamma_A(x) \vee \gamma_B(x) \rangle : x \in X \}; \quad [(iv)]$$

$$A \cup B = \{ \langle x, \mu_A(x) \vee \mu_B(x), \gamma_A(x) \wedge \gamma_B(x) \rangle : x \in X \}; [1]$$

The IFS's 0_{\sim} and 1_{\sim} are defined by , $0_{\sim} = \{ \langle x, 0, 1 \rangle : x \in X \}$ and

$$1_{\sim} = \{ \langle x, 1, 0 \rangle : x \in X \}. [3]$$

An intuitionistic fuzzy topology (IFT) in Coker's sense on a nonempty set X is a family T of intuitionistic fuzzy sets in X satisfying the following axioms: [(i)] $0_{\sim}, 1_{\sim} \in T$; [(ii)]

$$G_1 \cap G_2 \in T, \text{ for any } G_1, G_2 \in T;$$

$$[(iii)] \cup G_i \in T \text{ for arbitrary family } \{G_i : i \in J\} \subseteq T.$$

In this paper by (X, T) or simply by X we will denote the Coker's intuitionistic fuzzy topological space (IFTS). Each IFS which belongs to T is called an intuitionistic fuzzy open set (IFOS) in X .

The complement \bar{A} of an IFOS A in X is called an intuitionistic fuzzy closed set (IFCS) in X . [3] Let (X, T) be an IFTS and

$$A = \{ \langle x, \mu_A, \nu_A \rangle : x \in X \}$$

be an IFS in X . Then the intuitionistic fuzzy closure and intuitionistic fuzzy interior of A are defined by [(i)] $IFcl(A) = \bigcap \{C : C \text{ is an IFCS in } X \text{ and } C \supseteq A\}$; [(ii)]

$$IFint(A) = \bigcup \{D : D \text{ is an IFOS in } X \text{ and } D \subseteq A\}; [1]$$

For any IFS A in (X, T) we have [(i)] $cl(\bar{A}) = \overline{int(A)}$

$$[(ii)] int(\bar{A}) = \overline{cl(A)} [3]$$

Let $A, A_i (i \in J)$ be IFSs in X , $B, B_j (j \in K)$ IFSs in Y and

$$f : X \rightarrow Y \text{ a function. Then}$$

[(i)] $A \subseteq f^{-1}(f(A))$ (If f is injective, then $A = f^{-1}(f(A))$). [(ii)] $f(f^{-1}(B)) \subseteq B$ (If f is surjective, then $f(f^{-1}(B)) = B$).

$$[(iii)] f^{-1}(\cup B_j) = \cup f^{-1}(B_j).$$

$$[(iv)] f^{-1}(\cap B_j) = \cap f^{-1}(B_j).$$

$$[(v)] f^{-1}(1_{\sim}) = 1_{\sim}. \quad [(vi)] f^{-1}(0_{\sim}) = 0_{\sim}.$$

$$[(vii)] f^{-1}(\overline{B}) = \overline{f^{-1}(B)}. [4]$$

Let X be a nonempty set and $x \in X$ a fixed element in X . If $r \in I_0, s \in I_1$ are fixed real numbers

such that $r + s \leq 1$, then the IFS

$$x_{r,s} = \langle x, x_r, 1 - x_{1-s} \rangle$$

is called and intuitionistic fuzzy point (IFP) in X , where r

denotes the degree of membership of $x_{r,s}, s$

denotes the degree of non membership of $x_{r,s}$

and $x \in X$ the support of $x_{r,s}$. The IFP $x_{r,s}$ is

contained in the IFS $A(x_{r,s} \in A)$ if and only if

$$r < \mu_A(x), s > \gamma_A(x). [6]$$

An IFS U of an IFTS X is called [(i)] neighborhood of an IFP

$c(a, b)$, if there exists an IFOS G in X such that

$$c(a, b) \in G \leq U. \quad [(ii)] q\text{-neighborhood of an IFP } c(a, b),$$

if there exists an IFOS G in X such that $c(a, b) qG \leq U$.

[3] Let X and Y be two nonempty sets and $f : X \rightarrow Y$ be a function. [(i)] If

$$B = \{ \langle y, \mu_B(y), \gamma_B(y) \rangle : y \in Y \}$$

is an IFS in Y , then the preimage of B under f (denoted by

$$f^{-1}(B)) \text{ is defined by}$$

$$f^{-1}(B) = \{ \langle x, f^{-1}(\mu_B)(x), f^{-1}(\gamma_B)(x) \rangle : x \in X \}$$

[(ii)] If $A = \{ \langle x, \lambda_A(x), \nu_A(x) \rangle : x \in X \}$ is an IFS in X , then the image of A under f

(denoted by $f(A)$) is defined by

$$f(A) = \{ \langle y, f(\lambda_A(y)), (1 - f(1 - \nu_A))(y) \rangle : y \in Y \}.$$

[11] Let A be IFS in an IFTS (X, T) . A is called an [(i)] intuitionistic fuzzy regular open set (briefly IFROS) if $A = intcl(A)$ IFRCs) if $A = clint(A)$ [(ii)] intuitionistic fuzzy regular closed set (briefly IFRCs) if $A = clint(A)$. [2] Let (X, T) be a fuzzy topological space and λ be a fuzzy set in X . λ is called G_{δ} set if $\lambda = \bigwedge_{i=1}^{\infty} \lambda_i$ where each $\lambda_i \in T$. The complement of fuzzy G_{δ} is fuzzy F_{σ} . [5] A subset A of a space (X, T) is called locally closed (briefly lc) if $A = C \cap D$, where C is open and D is closed in (X, T) . [11] Let (X, T) be an IFTS and $A = \langle x, \mu_A(x), \nu_A(x) \rangle$ be a IFS in X . Then the fuzzy δ closure of A are denoted and defined by $cl_{\delta}(A) = \bigcap \{K : K \text{ is an IFRCs in } X \text{ and } A \subseteq K\}$ and

$int_{\delta}(A) = \cup\{G : G \text{ is an IFROS in } X \text{ and } G \subseteq A\}$. [10] Let A be an IFS in an IFTS (X, T) . A is called an intuitionistic fuzzy e -open set (IFeOS, for short) in X if $A \subseteq clint_{\delta}(A) \cup intcl_{\delta}(A)$ [8] Let (X, T) be an intuitionistic fuzzy topological space. Let $A = \{\langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X\}$ be an intuitionistic fuzzy set on an intuitionistic fuzzy topological space (X, T) . Then A is said to be intuitionistic fuzzy e -locally closed set (in short, IF- e -lcs) if $A = C \cap D$, where $C = \{\langle x, \mu_C(x), \gamma_C(x) \rangle : x \in X\}$ is an intuitionistic fuzzy e -open set and $D = \{\langle x, \mu_D(x), \gamma_D(x) \rangle : x \in X\}$ is an intuitionistic fuzzy e -closed set in (X, T) . [8] Let (X, T) be an intuitionistic fuzzy topological space. Let $A = \{\langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X\}$ be an intuitionistic fuzzy set on an intuitionistic fuzzy topological space X . Then A is said to be an intuitionistic fuzzy eG_{δ} -set if

$$A = \bigcap_{i=1}^{\infty} A_i,$$

where

$A_i = \{\langle x, \mu_{A_i}(x), \gamma_{A_i}(x) \rangle : x \in X\}$ is an intuitionistic fuzzy e -open set in an intuitionistic fuzzy topological space (X, T) .

[8] Let (X, T) be an intuitionistic fuzzy topological space. Let

$A = \{\langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X\}$ be an intuitionistic fuzzy set on an intuitionistic fuzzy topological space (X, T) . Then A is said to be an intuitionistic fuzzy eG_{δ} -locally closed set (in short, IF- eG_{δ} -lcs) if $A = C \cap D$, where $C = \{\langle x, \mu_C(x), \gamma_C(x) \rangle : x \in X\}$ is an intuitionistic fuzzy eG_{δ} set and $D = \{\langle x, \mu_D(x), \gamma_D(x) \rangle : x \in X\}$ is an intuitionistic fuzzy e -closed set in (X, T) . The complement of an intuitionistic fuzzy eG_{δ} -locally closed set is said to be an intuitionistic fuzzy eG_{δ} -locally open set (in short, IF- eG_{δ} -los). [8] Let (X, T) be an

intuitionistic fuzzy topological space. Let $A = \{\langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X\}$ be an intuitionistic fuzzy set on an intuitionistic fuzzy topological space (X, T) . Then A is said to be an intuitionistic fuzzy G_{δ} - e -locally closed set (in short, IF- G_{δ} - e -lcs) if $A = B \cap C$, where $B = \{\langle x, \mu_B(x), \gamma_B(x) \rangle : x \in X\}$ is an intuitionistic fuzzy G_{δ} set and $C = \{\langle x, \mu_C(x), \gamma_C(x) \rangle : x \in X\}$ is an intuitionistic fuzzy e -closed set in (X, T)

The complement of an intuitionistic fuzzy G_{δ} - e -locally closed set is said to be an intuitionistic fuzzy G_{δ} - e -locally open set (in short, IF- G_{δ} - e -los) [8] Let (X, T) be an intuitionistic fuzzy topological space. Let

$A = \{\langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X\}$ be an intuitionistic fuzzy set on an intuitionistic fuzzy topological space (X, T) . The intuitionistic fuzzy G_{δ} - e -locally closure of A is denoted and defined by IFG_{δ} - e - $lcl(A) = \bigcap\{B : B = \langle x, \mu_B(x), \gamma_B(x) \rangle : x \in X$ is an intuitionistic fuzzy G_{δ} - e -locally closed set in X and $A \subseteq B\}$. [8] Let (X, T) be an intuitionistic fuzzy topological space. Let

$A = \{\langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X\}$ be an intuitionistic fuzzy set on an intuitionistic fuzzy topological space (X, T) . The intuitionistic fuzzy G_{δ} - e -locally interior of A is denoted and defined by IFG_{δ} - e - $lint(A) = \bigcup\{B : B = \langle x, \mu_B(x), \gamma_B(x) \rangle : x \in X\}$

is an intuitionistic fuzzy G_{δ} - e -locally open set in X and $B \subseteq A$. [8] Let (X, T) be an intuitionistic fuzzy topological space. For any two intuitionistic fuzzy sets $A = \{\langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X\}$ and $B = \{\langle x, \mu_B(x), \gamma_B(x) \rangle : x \in X\}$ of an intuitionistic fuzzy topological space (X, T) then the following statements are true.

- (i) IFG_{δ} - e - $lcl(0) = 0$ (ii)
- $A \subseteq B \Rightarrow IFG_{\delta}$ - e - $lcl(A) \subseteq IFG_{\delta}$ - e - $lcl(B)$ (iii)

$$IFG_{\delta} - e - lcl(IFG_{\delta} - e - lcl(A)) = IFG_{\delta} - e - lcl(A) \quad (iv)$$

$$IFG_{\delta} - e - lcl(A \cup B) = (IFG_{\delta} - e - lcl(A)) \cup (IFG_{\delta} - e - lcl(B))$$

[8] [(i)] $IFG_{\delta} - e - lcl(A) = A$ if and only if A is an intuitionistic fuzzy $G_{\delta} - e$ -locally closed set [(ii)] $IFG_{\delta} - lint(A) \subseteq A \subseteq IFG_{\delta} - e - lcl(A)$ [(iii)] $IFG_{\delta} - e - lint(1_{\sim}) = 1_{\sim}$ [(iv)] $IFG_{\delta} - lint(0_{\sim}) = 0_{\sim}$

[(v)] $IFG_{\delta} - e - lcl(1_{\sim}) = 1_{\sim}$ [3] Let (X, T) and (Y, S) be two IFT's and let $f : X \rightarrow Y$ be a function. Then f is said to be intuitionistic fuzzy continuous iff the preimage of each IFS in S is an IFS in T . [10] Let (X, T) and (Y, S) be two IFT's and let $f : X \rightarrow Y$ be a function. Then f is said to be intuitionistic fuzzy e -continuous iff the preimage of each IFS in S is an IFeOS in T .

3 Intuitionistic fuzzy $G_{\delta} - e$ - locally function

DEFINITION. 3.1 Let (X, T) and (Y, S) be any two intuitionistic fuzzy topological spaces. Let $f : (X, T) \rightarrow (Y, S)$ be an intuitionistic fuzzy mapping. Then f is said to be an [(i)] intuitionistic fuzzy $G_{\delta} - e$ - locally function, if for each intuitionistic fuzzy closed set A in an intuitionistic fuzzy topological space (X, T) , $f(A)$ is an intuitionistic fuzzy $G_{\delta} - e$ -locally closed set in an intuitionistic fuzzy topological space (Y, S) . [(ii)] intuitionistic fuzzy strongly $G_{\delta} - e$ -locally function, if for each intuitionistic fuzzy $G_{\delta} - e$ -closed set A in an intuitionistic fuzzy topological space (X, T) , $f(A)$ is an intuitionistic fuzzy $G_{\delta} - e$ -locally closed set in an intuitionistic fuzzy topological space (Y, S) .

THEOREM.3.1 Let (X, T) and (Y, S) be any two intuitionistic fuzzy topological spaces. Let $f : (X, T) \rightarrow (Y, S)$ be an intuitionistic fuzzy mapping. Then the following statements are equivalent (i) f is an intuitionistic fuzzy $G_{\delta} - e$ -locally function (ii) for each

intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (Y, S) and each intuitionistic fuzzy closed set B of an intuitionistic fuzzy topological space (X, T) with $f^{-1}(A) \subseteq B$, there is an intuitionistic fuzzy $G_{\delta} - e$ -locally closed set C of an intuitionistic fuzzy topological space (Y, S) with $A \subseteq C$ such that $f^{-1}(C) \subseteq B$. (iii) $f^{-1}(IFG_{\delta} - e - lcl(A)) \subseteq IFcl(f^{-1}(A))$,

for each intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (Y, S) . (iv) $f(IFint(B)) \subseteq IFG_{\delta} - e - lint(f(B))$, for each intuitionistic fuzzy set B of an intuitionistic fuzzy topological space (X, T) .

Proof. (i) \Rightarrow (ii): Suppose f is an intuitionistic fuzzy $G_{\delta} - e$ -locally function. Let A be any intuitionistic fuzzy set A in an intuitionistic fuzzy topological space (Y, S) . Let B be any intuitionistic fuzzy closed in an intuitionistic fuzzy topological space (X, T) such that $f^{-1}(A) \subseteq B$. Let $C = \overline{f(B)}$. Then C is an intuitionistic fuzzy $G_{\delta} - e$ -locally closed set in an intuitionistic fuzzy topological space (Y, S) and $A \subseteq C$. We have, $f^{-1}(C) = f^{-1}(\overline{f(B)}) = \overline{f^{-1}(f(B))} \subseteq B$.

Therefore, $f^{-1}(C) \subseteq B$. (ii) \Rightarrow (i): Let D be an intuitionistic fuzzy open set in an intuitionistic fuzzy topological space (X, T) .

Put $A = \overline{f(D)}$ and $B = \overline{D}$. Thus $f^{-1}(A) = f^{-1}(\overline{f(D)}) = \overline{f^{-1}(f(D))} \subseteq \overline{D}$. By hypothesis, there exists an intuitionistic fuzzy topological space (Y, S) with $A \subseteq C$ such that $f^{-1}(C) \subseteq B = \overline{D}$. Then, $\overline{f^{-1}(C)} \supseteq D \Rightarrow D \subseteq f^{-1}(\overline{C})$. Hence, $f(D) \subseteq f(f^{-1}(\overline{C})) \subseteq \overline{C}$ (3.1) Also, since $A \subseteq C$, we have $\overline{f(D)} \subseteq C$. This implies $f(D) \supseteq \overline{C}$. (3.2) From (3.1) and (3.2), we get $f(D) = \overline{C}$ is an intuitionistic fuzzy $G_{\delta} - e$ -locally closed set in an intuitionistic fuzzy topological space (Y, S) . Hence f is an intuitionistic fuzzy $G_{\delta} - e$ -locally function. (ii) \Rightarrow (iii): Let A be an intuitionistic

fuzzy set in an intuitionistic fuzzy topological space (Y, S) . Since $IFcl(f^{-1}(A))$ is an intuitionistic fuzzy closed set in an intuitionistic fuzzy topological space (X, T) with $f^{-1}(A) \subseteq IFcl(f^{-1}(A))$. Then by (ii), there is an intuitionistic fuzzy G_δ - e -locally closed set C in an intuitionistic fuzzy topological space (Y, S) with $A \subseteq C, f^{-1}(IFG_\delta$ - e - $lcl(A)) \subseteq IFG_\delta$ - e - $lcl(C) \subseteq f^{-1}(C) \subseteq IFcl(f^{-1}(A))$.

Therefore, $f^{-1}(IFG_\delta$ - e - $lcl(A)) \subseteq IFcl(f^{-1}(A))$. (iii) \Rightarrow (iv):

$f^{-1}(IFG_\delta$ - e - $lcl(A)) \subseteq IFcl(f^{-1}(A))$, for each intuitionistic fuzzy set A of an intuitionistic fuzzy topological space (Y, S) .

Putting $A = \overline{f(B)}, f^{-1}(IFG_\delta$ - e - $lcl(\overline{f(B)}) \subseteq IFcl(f^{-1}(\overline{f(B)})) \subseteq IFcl(f^{-1}(f(\overline{B}))) \subseteq IFcl(\overline{B}) \subseteq \overline{IFint(B)}$,

$f^{-1}(\overline{IFG_\delta$ - e - $lint(f(B))}) \subseteq \overline{IFint(B)}$

Taking complement on both sides, $\overline{f^{-1}(\overline{IFG_\delta$ - e - $lint(f(B))})} \subseteq \overline{IFint(B)}$,

$f^{-1}(IFG_\delta$ - e - $lint(f(B))) \supseteq IFint(B)$

Therefore, $f(IFint(B)) \subseteq IFG_\delta$ - e - $lint(f(B))$. (iv) \Rightarrow (i): It is obvious.

DEFINITION.3.2 Let (X, T) and (Y, S) be any two intuitionistic fuzzy topological spaces. Let $f : (X, T) \rightarrow (Y, S)$ be an intuitionistic fuzzy mapping. Then f is said to be an intuitionistic fuzzy G_δ - e -locally homeomorphism if f is one to one, onto, intuitionistic fuzzy G_δ - e -locally irresolute function and intuitionistic fuzzy strongly G_δ - e -locally function.

THEOREM.3.2 Let (X, T) and (Y, S) be any two intuitionistic fuzzy topological spaces. If $f : (X, T) \rightarrow (Y, S)$ is an intuitionistic fuzzy G_δ - e -locally homeomorphism. Then the following statements are valid. (i) For any intuitionistic fuzzy set A in an intuitionistic fuzzy topological space (X, T) , IFG_δ - e - $lcl(f(A)) = f(IFG_\delta$ - e - $lcl(A))$. (ii) For any intuitionistic fuzzy set A in an

intuitionistic fuzzy topological space (X, T) , $f(\overline{IFG_\delta$ - e - $0e0lint((\overline{A}))}) = \overline{IFG_\delta$ - e - $0e0lint(f(\overline{A}))}$

(iii) For any intuitionistic fuzzy set A in an intuitionistic fuzzy topological space (Y, S) , IFG_δ - e - $lcl(f^{-1}(A)) = f^{-1}(IFG_\delta$ - e - $lcl(A))$. (iv) For any intuitionistic fuzzy set A in an intuitionistic fuzzy topological space (Y, S) ,

$$f^{-1}(\overline{IFG_\delta$$
- e - $0e0lint((\overline{A}))}) = \overline{IFG_\delta$ - e - $0e0lint(f^{-1}(\overline{A}))}$

Proof. (i) Let A be any intuitionistic fuzzy set in an intuitionistic fuzzy topological space (X, T) . Since f is an intuitionistic fuzzy G_δ - e -locally irresolute function. By (ii) and (iii) of Theorem 3.5[9] $f(IFG_\delta$ - e - $lcl(A)) \subseteq IFG_\delta$ - e - $lcl(f(A))$ (3.3)

$$IFG_\delta$$
- e - $lcl(f(A)) \subseteq f(IFG_\delta$ - e - $lcl(A))$ (3.4)

From (3.3) and (3.4) implies that IFG_δ - e - $lcl(f(A)) = f(IFG_\delta$ - e - $lcl(A))$. (ii) Let A be any intuitionistic fuzzy set in an intuitionistic fuzzy topological space (X, T) . Since f is an intuitionistic fuzzy G_δ - e -locally homeomorphism. Then by above condition (ii), IFG_δ - e - $lcl(f(A)) = f(IFG_\delta$ - e - $lcl(A))$. Now,

$$\overline{IFG_\delta$$
- e - $lint(f(A))} = \overline{f(IFG_\delta$ - e - $lint(A))},$

$$f(\overline{IFG_\delta$$
- e - $lint(A)}) = \overline{IFG_\delta$ - e - $lint(f(A))}.$

(iii) Let A be any intuitionistic fuzzy set in an intuitionistic fuzzy topological space (Y, S) . Since f is an intuitionistic fuzzy G_δ - e -locally homeomorphism. Since f is an intuitionistic fuzzy strongly G_δ - e -locally function. Also f^{-1} is an intuitionistic fuzzy G_δ - e -locally irresolute function. By (ii) and (iii) of Theorem 3.5[9]

$$IFG_\delta$$
- e - $lcl(f^{-1}(A)) \subseteq f^{-1}(IFG_\delta$ - e - $lcl(A))$ (3.5)

$$f^{-1}(IFG_\delta$$
- e - $lcl(A)) \subseteq IFG_\delta$ - e - $lcl(f^{-1}(A))$ (3.6)

From (3.5) and (3.6) implies that IFG_δ - e - $lcl(f^{-1}(A)) = f^{-1}(IFG_\delta$ - e - $lcl(A))$. (iv) Let A be any intuitionistic fuzzy set in an

intuitionistic fuzzy topological space (Y, S) . Since f is an intuitionistic fuzzy G_δ - e -locally homeomorphism. Then by above condition (iii), IFG_δ - e -

$$lcl(f^{-1}(A)) = f^{-1}(IFG_\delta$$
- e - $lcl(A))$. Taking complement on bothsides,
$$\overline{IFG_\delta$$
- e - $lcl(f^{-1}(A))} = \overline{f^{-1}(IFG_\delta$ - e - $lcl(A))}$,
$$f^{-1}(\overline{IFG_\delta$$
- e - $lcl(A)}) = \overline{IFG_\delta$ - e - $lcl(f^{-1}(A))}$.

THEOREM.3.3 Let (X, T) , (Y, S) and (Z, R) be any three intuitionistic fuzzy topological spaces. If $f : (X, T) \rightarrow (Y, S)$ and $g : (Y, S) \rightarrow (Z, R)$ be any two intuitionistic fuzzy mappings. Then the following statements are valid. [(i)]If f is an intuitionistic fuzzy G_δ - e -locally irresolute function and g is an intuitionistic fuzzy G_δ - e -locally continuous function, then $g \circ f$ is an intuitionistic fuzzy G_δ - e -locally continuous function. [(ii)]If f is an intuitionistic fuzzy G_δ - e -locally continuous function and g is an intuitionistic fuzzy weakly G_δ - e -locally continuous function, then $g \circ f$ is an intuitionistic fuzzy G_δ - e -locally irresolute function.

Proof. (i) Let A be any intuitionistic fuzzy closed set in an intuitionistic fuzzy topological space (Z, R) . Since g is an intuitionistic fuzzy G_δ - e -locally continuous function, $g^{-1}(A)$ is an intuitionistic fuzzy G_δ - e -locally closed set in an intuitionistic fuzzy topological space (Y, S) . Since f is an intuitionistic fuzzy G_δ - e -locally irresolute function, $f^{-1}(g^{-1}(A))$ is an intuitionistic fuzzy G_δ - e -locally closed set in an intuitionistic fuzzy topological space (X, T) . Now, $(g \circ f)^{-1}(A) = f^{-1}(g^{-1}(A))$ is an intuitionistic fuzzy G_δ - e -locally closed set in an intuitionistic fuzzy topological space (X, T) . Hence, $g \circ f$ is an intuitionistic fuzzy G_δ - e -locally continuous function. (ii) Let A

be any intuitionistic fuzzy G_δ - e -locally closed set in an intuitionistic fuzzy topological space (Z, R) . Since g is an intuitionistic fuzzy weakly G_δ - e -locally continuous function, $g^{-1}(A)$ is an intuitionistic fuzzy closed set in an intuitionistic fuzzy topological space (Y, S) . Since f is an intuitionistic fuzzy G_δ - e -locally continuous function, $f^{-1}(g^{-1}(A))$ is an intuitionistic fuzzy G_δ - e -locally closed set in an intuitionistic fuzzy topological space (X, T) . Now $(g \circ f)^{-1}(A) = f^{-1}(g^{-1}(A))$ is an intuitionistic fuzzy G_δ - e -locally closed set in an intuitionistic fuzzy topological space (X, T) . Hence, $g \circ f$ is an intuitionistic fuzzy G_δ - e -locally irresolute function.

DEFINITION.3.3 An intuitionistic fuzzy topological space (X, T) is said to be an intuitionistic fuzzy G_δ - e -local T_2 space if and only if for every intuitionistic fuzzy points $c_{r,s}$ and $d_{m,n}$ in an intuitionistic fuzzy topological space (X, T) and $c \neq d$ there exists an intuitionistic fuzzy G_δ - e -locally open sets $G = \langle x, \mu_G, \gamma_G \rangle, H = \langle x, \mu_H, \gamma_H \rangle$ with $\mu_G(c) = 0, \gamma_G(c) = 1, \mu_H(d) = 1, \gamma_H(d) = 0$ and $G \cap H = 0$.

PROPOSITION.3.1 Let (X, T) and (Y, S) be any two intuitionistic fuzzy topological spaces. Let $f : (X, T) \rightarrow (Y, S)$ be an intuitionistic fuzzy injective mapping and intuitionistic fuzzy G_δ - e -locally continuous function. If (Y, S) is an intuitionistic fuzzy T_2 space, then (X, T) is an intuitionistic fuzzy G_δ - e -local T_2 space.

Proof. Let $c_{r,s}$ and $d_{m,n}$ be an intuitionistic fuzzy points in an intuitionistic fuzzy topological space (X, T) and $c \neq d$. By intuitionistic fuzzy injective function of f , we have $f(c) \neq f(d)$. Since, (Y, S) is an intuitionistic fuzzy T_2 space, there exists an intuitionistic fuzzy open sets $G = \langle y, \mu_G, \gamma_G \rangle, H = \langle y, \mu_H, \gamma_H \rangle$ of S with

$$\mu_G(f(c)) = 0, \gamma_G(f(c)) = 1, \mu_H(f(d)) = 1, \gamma_H(f(d)) = 0$$

and $G \cap H = 0_{\sim}$. Since f is an intuitionistic fuzzy G_{δ} - e -locally continuous function. This

implies
$$f^{-1}(G) = \langle x, f^{-1}(\mu_G), f^{-1}(\gamma_G) \rangle,$$

$$f^{-1}(H) = \langle x, f^{-1}(\mu_H), f^{-1}(\gamma_H) \rangle$$

and $N^{IFG_{\delta}-e-lq}(c_{r,s})$ and $N^{IFG_{\delta}-e-lq}(d_{m,n})$ respectively. That is, $f^{-1}(G)$ and $f^{-1}(H)$ are intuitionistic fuzzy G_{δ} - e -locally open

sets.

Now

$$f^{-1}(\mu_G)(c_{r,s}) = \mu_G(f(c)) = 0, f^{-1}(\gamma_G)(c_{r,s}) = \gamma_G(f(c)) = 1, f^{-1}(\mu_H)(d_{m,n}) = \mu_H(f(d)) = 1, f^{-1}(\gamma_H)(d_{m,n}) = \gamma_H(f(d)) = 0,$$

$$f^{-1}(G) \cap f^{-1}(H) = f^{-1}(G \cap H) = f^{-1}(0_{\sim}) = 0_{\sim}$$

. Hence, (X, T) is an intuitionistic fuzzy G_{δ} - e -local T_2 space.

PROPOSITION.3.2 Let (X, T) and (Y, S) be any two intuitionistic fuzzy topological spaces. Let $f : (X, T) \rightarrow (Y, S)$ be an intuitionistic fuzzy injective mapping and intuitionistic fuzzy weakly G_{α} - e -locally continuous function. If (Y, S) is an intuitionistic fuzzy G_{α} - e -local T_2 space, then (X, T) is an intuitionistic fuzzy T_2 space.

Proof. Let $c_{r,s}$ and $d_{m,n}$ be an intuitionistic fuzzy points in an intuitionistic fuzzy topological space (X, T) and $c \neq d$. By intuitionistic fuzzy injective function of f , we have $f(c) \neq f(d)$. Since, (Y, S) is an intuitionistic fuzzy G_{δ} - e -local T_2 space, there exists an intuitionistic fuzzy G_{δ} - e -locally open sets $G = \langle y, \mu_G, \gamma_G \rangle, H = \langle y, \mu_H, \gamma_H \rangle$ of S with $\mu_G(f(c)) = 0, \gamma_G(f(c)) = 1, \mu_H(f(d)) = 1, \gamma_H(f(d)) = 0$ and $G \cap H = 0_{\sim}$. Since f is an intuitionistic fuzzy weakly G_{δ} - e -locally continuous function. This implies

$$f^{-1}(G) = \langle x, f^{-1}(\mu_G), f^{-1}(\gamma_G) \rangle,$$

are

$$f^{-1}(H) = \langle x, f^{-1}(\mu_H), f^{-1}(\gamma_H) \rangle$$

$N(c_{r,s})$ and $N(d_{m,n})$ respectively. That is $f^{-1}(G)$ and $f^{-1}(H)$ are intuitionistic fuzzy open sets. Now,

$$f^{-1}(\mu_G)(c_{r,s}) = \mu_G(f(c)) = 0, f^{-1}(\gamma_G)(c_{r,s}) = \gamma_G(f(c)) = 1, f^{-1}(\mu_H)(d_{m,n}) = \mu_H(f(d)) = 1, f^{-1}(\gamma_H)(d_{m,n}) = \gamma_H(f(d)) = 0$$

and

$$f^{-1}(G) \cap f^{-1}(H) = f^{-1}(G \cap H) = f^{-1}(0_{\sim}) = 0_{\sim}$$

. Hence, (X, T) is an intuitionistic fuzzy T_2 space.

DEFINITION.3.4 An intuitionistic fuzzy topological space (X, T) is said to be an intuitionistic fuzzy G_{δ} - e -local Urysohn space if and only if for every intuitionistic fuzzy points $c_{r,s}$ and $d_{m,n}$ in an intuitionistic fuzzy topological space (X, T) and $c \neq d$ there exists an intuitionistic fuzzy G_{δ} - e -locally open sets $G = \langle x, \mu_G, \gamma_G \rangle, H = \langle x, \mu_H, \gamma_H \rangle$ with $\mu_G(c) = 0, \gamma_G(c) = 1, \mu_H(d) = 1, \gamma_H(d) = 0$ and $IFG_{\delta}-e-lcl(G) \cap IFG_{\delta}-e-lcl(H) = 0_{\sim}$.

PROPOSITION.3.3 Every intuitionistic fuzzy G_{δ} - e -local Urysohn space is an intuitionistic fuzzy G_{δ} - e -local T_2 space.

Proof. Let (X, T) be an intuitionistic fuzzy G_{δ} - e -local Urysohn space. Then for every intuitionistic fuzzy points $c_{r,s}$ and $d_{m,n}$ in an intuitionistic fuzzy topological space (X, T) and $c \neq d$ there exists an intuitionistic fuzzy G_{δ} - e -locally open sets $G = \langle x, \mu_G, \gamma_G \rangle, H = \langle x, \mu_H, \gamma_H \rangle$ with $\mu_G(c) = 0, \gamma_G(c) = 1, \mu_H(d) = 1, \gamma_H(d) = 0$ and $IFG_{\delta}-e-lcl(G) \cap IFG_{\delta}-e-lcl(H) = 0_{\sim}$. Since $G \subseteq IFG_{\delta}-e-lcl(G)$ and $H \subseteq IFG_{\delta}-e-lcl(H)$. Then $G \cap H \subseteq IFG_{\delta}-e-lcl(G) \cap IFG_{\delta}-e-$

$lcl(H)$. This implies $G \cap H = 0$. Hence (X, T) is an intuitionistic fuzzy G_δ - e -local T_2 space..

Interraltion

DEFINITION.4.1 Let (X, T) and (Y, S) be two IFT's and let $f : X \rightarrow Y$ be a function. Then f is said to be an [(i)]intuitionistic fuzzy e -locally continuous iff the preimage of each IFCS in S is an intuitionistic fuzzy e -locally closed set in T . [(ii)]intuitionistic fuzzy G_δ - e -locally continuous iff the preimage of each IFCS in S is an intuitionistic fuzzy G_δ - e -locally closed set in T . [(iii)]intuitionistic fuzzy eG_δ -locally continuous iff the preimage of each IFCS in S is an intuitionistic fuzzy eG_δ -locally closed set in T .

PROPOSITION.4.1 Let (X, T) and (Y, S) be two intuitionistic fuzzy topological spaces. Let $f : (X, T) \rightarrow (Y, S)$ be an intuitionistic fuzzy G_δ -locally continuous function. Then f is an intuitionistic fuzzy G_δ - e -locally continuous function.

Proof. Let A be an intuitionistic fuzzy closed set in an intuitionistic fuzzy topological space (Y, S) . Since f is an intuitionistic fuzzy G_δ -locally continuous function, $f^{-1}(A)$ is an intuitionistic fuzzy G_δ - e -locally closed set in an intuitionistic fuzzy topological space (X, T) . Since every intuitionistic fuzzy G_δ -locally closed set is an intuitionistic fuzzy G_δ - e -locally closed set, $f^{-1}(A)$ is also an intuitionistic fuzzy G_δ - e -locally closed set. Hence f is an intuitionistic fuzzy G_δ - e -locally continuous function.

EXAMPLE.4.1 Let $X = \{a, b\} = Y$,

$$A = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle$$

$$B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \vee B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \wedge B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$C = \left\langle x, \left(\frac{a}{1}, \frac{b}{1}\right), \left(\frac{a}{0}, \frac{b}{0.1}\right) \right\rangle. \text{ Now, the family}$$

$T = \{0_-, 1_-, A, B, A \vee B, A \wedge B\}$ of IFS's in X is an IFT on X and the family $S = \{0_-, 1_-, C\}$ of IFS's in Y is an IFT on Y . If we define the function $f : X \rightarrow Y$ be the identity function, then $f^{-1}(\bar{C})$ is an IFG_δ -locally continuous but not IFe -locally continuous.

EXAMPLE.4.2 Let $X = \{a, b\} = Y$,

$$A = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \vee B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \wedge B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$D = \left\langle x, \left(\frac{a}{0.7}, \frac{b}{0.7}\right), \left(\frac{a}{0}, \frac{b}{0.1}\right) \right\rangle. \text{ Now, the}$$

family $T = \{0_-, 1_-, A, B, A \vee B, A \wedge B\}$ of IFS's in X is an IFT on X and the family $S = \{0_-, 1_-, D\}$ of IFS's in Y is an IFT on Y . If we define the function $f : X \rightarrow Y$ be the identity function, then $f^{-1}(\bar{D})$ is an IFG_δ - e -locally continuous but not IFG_δ -locally continuous.

EXAMPLE.4.3 Let $X = \{a, b\} = Y$,

$$A = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \vee B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \wedge B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$E = \left\langle x, \left(\frac{a}{0.5}, \frac{b}{0.5}\right), \left(\frac{a}{0}, \frac{b}{0.1}\right) \right\rangle. \text{ Now, the}$$

family $T = \{0_-, 1_-, A, B, A \vee B, A \wedge B\}$ of IFS's in X is an IFT on X and the family

$S = \{0_-, 1_-, E\}$ of IFS's in Y is an IFT on Y .
 If we define the function $f : X \rightarrow Y$ be the identity function, then $f^{-1}(\bar{E})$ is an IF e -locally continuous but not IF G_δ - e -locally continuous.

EXAMPLE.4.4 Let $X = \{a, b\} = Y$,

$$A = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \vee B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \wedge B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$F = \left\langle x, \left(\frac{a}{0.6}, \frac{b}{0.6}\right), \left(\frac{a}{0.1}, \frac{b}{0.1}\right) \right\rangle. \text{ Now, the}$$

family $T = \{0_-, 1_-, A, B, A \vee B, A \wedge B\}$ of IFS's in X is an IFT on X and the family $S = \{0_-, 1_-, F\}$ of IFS's in Y is an IFT on Y .

If we define the function $f : X \rightarrow Y$ be the identity function, then $f^{-1}(\bar{E})$ is an IF G_δ - e -locally continuous but not IF- e -locally continuous.

EXAMPLE.4.5 Let $X = \{a, b\} = Y$,

$$A = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \vee B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \wedge B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$G = \left\langle x, \left(\frac{a}{0.9}, \frac{b}{0.9}\right), \left(\frac{a}{0}, \frac{b}{0.1}\right) \right\rangle. \text{ Now, the}$$

family $T = \{0_-, 1_-, A, B, A \vee B, A \wedge B\}$ of IFS's in X is an IFT on X and the family $S = \{0_-, 1_-, G\}$ of IFS's in Y is an IFT on Y .

If we define the function $f : X \rightarrow Y$ be the identity function, then $f^{-1}(\bar{G})$ is an IF eG_δ -locally continuous but not IF G_δ - e -locally continuous.

EXAMPLE.4.6 Let $X = \{a, b\} = Y$,

$$A = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \vee B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \wedge B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$G = \left\langle x, \left(\frac{a}{0.9}, \frac{b}{0.9}\right), \left(\frac{a}{0}, \frac{b}{0.1}\right) \right\rangle. \text{ Now, the}$$

family $T = \{0_-, 1_-, A, B, A \vee B, A \wedge B\}$ of IFS's in X is an IFT on X and the family $S = \{0_-, 1_-, G\}$ of IFS's in Y is an IFT on Y .

If we define the function $f : X \rightarrow Y$ be the identity function, then $f^{-1}(\bar{G})$ is an IF eG_δ -locally continuous but not IF G_δ -locally continuous.

EXAMPLE.4.7 Let $X = \{a, b\} = Y$,

$$A = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \vee B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \wedge B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$H = \left\langle x, \left(\frac{a}{0.6}, \frac{b}{0.6}\right), \left(\frac{a}{0.3}, \frac{b}{0.1}\right) \right\rangle. \text{ Now, the}$$

family $T = \{0_-, 1_-, A, B, A \vee B, A \wedge B\}$ of IFS's in X is an IFT on X and the family $S = \{0_-, 1_-, H\}$ of IFS's in Y is an IFT on Y .

If we define the function $f : X \rightarrow Y$ be the identity function, then $f^{-1}(\bar{H})$ is an IF G_δ -locally continuous but not IF eG_δ -locally continuous.

EXAMPLE.4.8 Let $X = \{a, b\} = Y$,

$$A = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3}\right), \left(\frac{a}{0.6}, \frac{b}{0.6}\right) \right\rangle,$$

$$B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1}\right), \left(\frac{a}{0.5}, \frac{b}{0.4}\right) \right\rangle,$$

$$A \vee B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.3} \right), \left(\frac{a}{0.5}, \frac{b}{0.4} \right) \right\rangle,$$

$$A \wedge B = \left\langle x, \left(\frac{a}{0.3}, \frac{b}{0.1} \right), \left(\frac{a}{0.6}, \frac{b}{0.6} \right) \right\rangle,$$

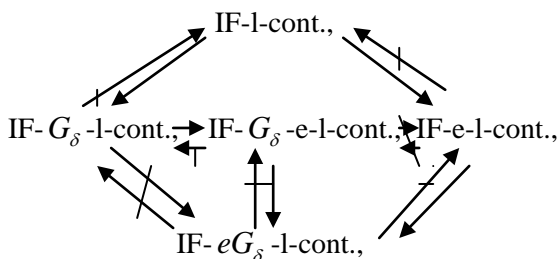
$$I = \left\langle x, \left(\frac{a}{0.5}, \frac{b}{0.4} \right), \left(\frac{a}{0}, \frac{b}{0.1} \right) \right\rangle$$

Now, the family $T = \{0_-, 1_-, A, B, A \vee B, A \wedge B\}$ of IFS's in X is an IFT on X and the family $S = \{0_-, 1_-, I\}$ of IFS's in Y is an IFT on Y .

If we define the function $f : X \rightarrow Y$ be the identity function, then $f^{-1}(\bar{I})$ is an Ife-locally continuous but not IF-locally continuous.

REMARK.4.1 Every intuitionistic fuzzy locally continuous is an intuitionistic fuzzy G_δ -locally continuous but the converse need not be true as shown in [7]

REMARK.4.2 Clearly the following diagram holds.



DEFINITION.4.2 An intuitionistic fuzzy topological space (X, T) is said to be intuitionistic fuzzy G_δ - e -local connected if and only if the only intuitionistic fuzzy sets which are both intuitionistic fuzzy G_δ - e -locally open set and intuitionistic fuzzy G_δ - e -locally closed set are 0_- and 1_- .

PROPOSITION.4.2 Let (X, T) and (Y, S) be any two intuitionistic fuzzy topological spaces. If $f : (X, T) \rightarrow (Y, S)$ is an intuitionistic fuzzy G_δ - e -locally continuous surjective function and (X, T) is an intuitionistic fuzzy G_δ - e -local connected space then (Y, S) is an intuitionistic fuzzy connected space.

Proof. Let (X, T) be an intuitionistic fuzzy G_δ - e -local connected space. Suppose that (Y, S) is not an intuitionistic fuzzy connected

space. Then there exists a proper intuitionistic fuzzy set A such that A is both intuitionistic fuzzy open set and intuitionistic fuzzy closed set in (Y, S) . Since f is an intuitionistic fuzzy G_δ - e -locally continuous surjective function, then $f^{-1}(A)$ is both intuitionistic fuzzy G_δ - e -locally open set and intuitionistic fuzzy G_δ - e -locally closed set in (X, T) , which is contradiction. Hence, (Y, S) is an intuitionistic fuzzy connected space.

DEFINITION.4.3 Let (X, T) be an intuitionistic fuzzy topological space. If a family $\{\langle x, \mu_{G_j}, \gamma_{G_j} \rangle : j \in J\}$ of an intuitionistic fuzzy G_δ - e -locally open sets in X satisfies the condition $\bigcup \{\langle x, \mu_{G_j}, \gamma_{G_j} \rangle : j \in J\} = 1_-$ then it is called as an intuitionistic fuzzy G_δ - e -locally open cover of an intuitionistic fuzzy topological space (X, T) .

DEFINITION.4.4 An intuitionistic fuzzy topological space (X, T) is said to be intuitionistic fuzzy G_δ - e -local compact if every intuitionistic fuzzy G_δ - e -locally open cover of $\{A_j : j \in J\}$ of an intuitionistic fuzzy topological space (X, T) , there exists a finite subfamily $J_0 \subset J$ such that $1_- = \bigcup \{A_j : j \in J_0\}$

PROPOSITION.4.3 Let (X, T) and (Y, S) be any two intuitionistic fuzzy topological spaces. If $f : (X, T) \rightarrow (Y, S)$ is an intuitionistic fuzzy G_δ - e -locally continuous bijective function and (X, T) is an intuitionistic fuzzy G_δ - e -local compact space then (Y, S) is an intuitionistic fuzzy G_δ - e -local compact space.

Proof Let $\{A_j : j \in J\}$ be an intuitionistic fuzzy open cover of an intuitionistic fuzzy topological space (Y, S) such that $1_- = \bigcup_{j \in J} A_j$ Since f is an intuitionistic fuzzy G_δ - e -locally continuous bijective function, $\{f^{-1}(A_j) : j \in J\}$ is an intuitionistic fuzzy

G_δ - e -locally open cover of an intuitionistic fuzzy topological space (X, T) . From, (ref{6e})

$$f^{-1} = f^{-1}(\bigcup_{j \in J} A_j), 1_{\sim} = \bigcup_{j \in J} f^{-1}(A_j). \quad \text{Now}$$

$\{f^{-1}(A_j) : j \in J\}$ is an intuitionistic fuzzy G_δ - e -locally open cover of an intuitionistic fuzzy topological space (X, T) . Since (X, T) is an intuitionistic fuzzy G_δ - e -local compact space, then there exist a finite subcover $\{f^{-1}(A_j) : j = 1, 2, 3, \dots, n\}$ of $\{f^{-1}(A_j) : j \in J\}$ is an intuitionistic fuzzy topological space (X, T) . Then,

$$1_{\sim} = \bigcup_{j=1}^n f^{-1}(A_j). \quad \text{Now,}$$

$f(1_{\sim}) = f(\bigcup_{j=1}^n f^{-1}(A_j))$. Since f is an intuitionistic fuzzy surjective

$$\text{function, } 1_{\sim} = \bigcup_{j=1}^n f(f^{-1}(A_j)) = \bigcup_{j=1}^n A_j \text{ implies}$$

that (Y, S) is an intuitionistic fuzzy G_δ - e -local compact space.

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